

Atmospheric Stability and weakening of tropical circulation

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Global water vapor budget (Held and Soden 2006):

$$P \approx Mq$$

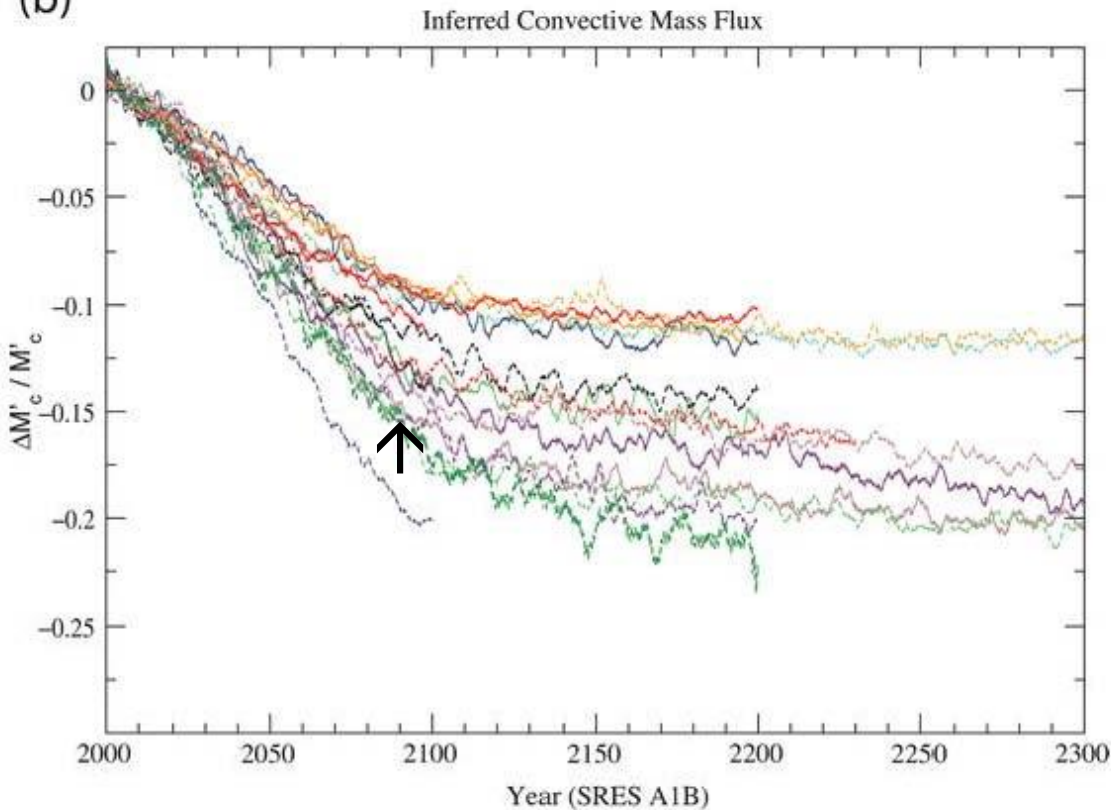
$$\rightarrow \delta P \approx \underbrace{M \delta q}_{\text{thermodynamic}} + \underbrace{q \delta M}_{\text{dynamic}}$$

P : precipitation

M : mass flux; q : PBL water vapor

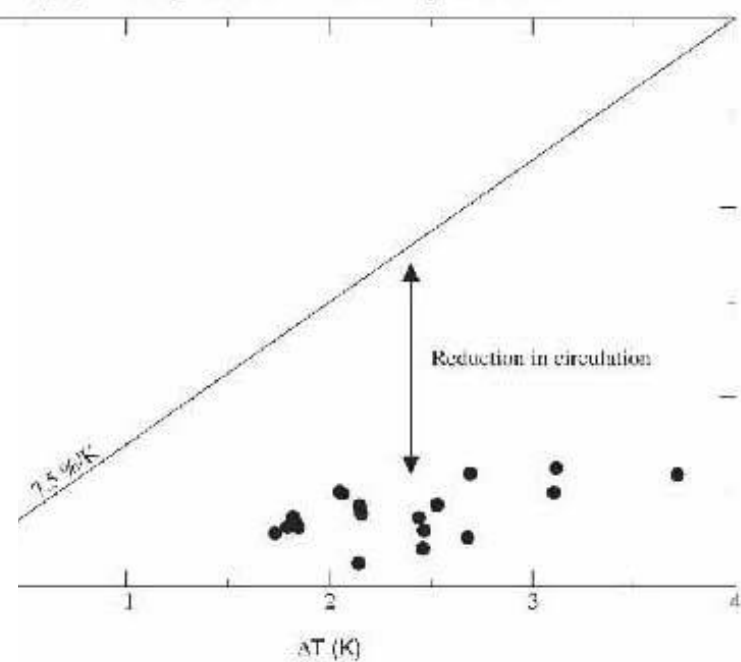
(a) Atmospheric Water vs. Temperature

(b)



7.5% in q per 1°C T
(Clausius-Clapeyron) \rightarrow
thermodynamic component

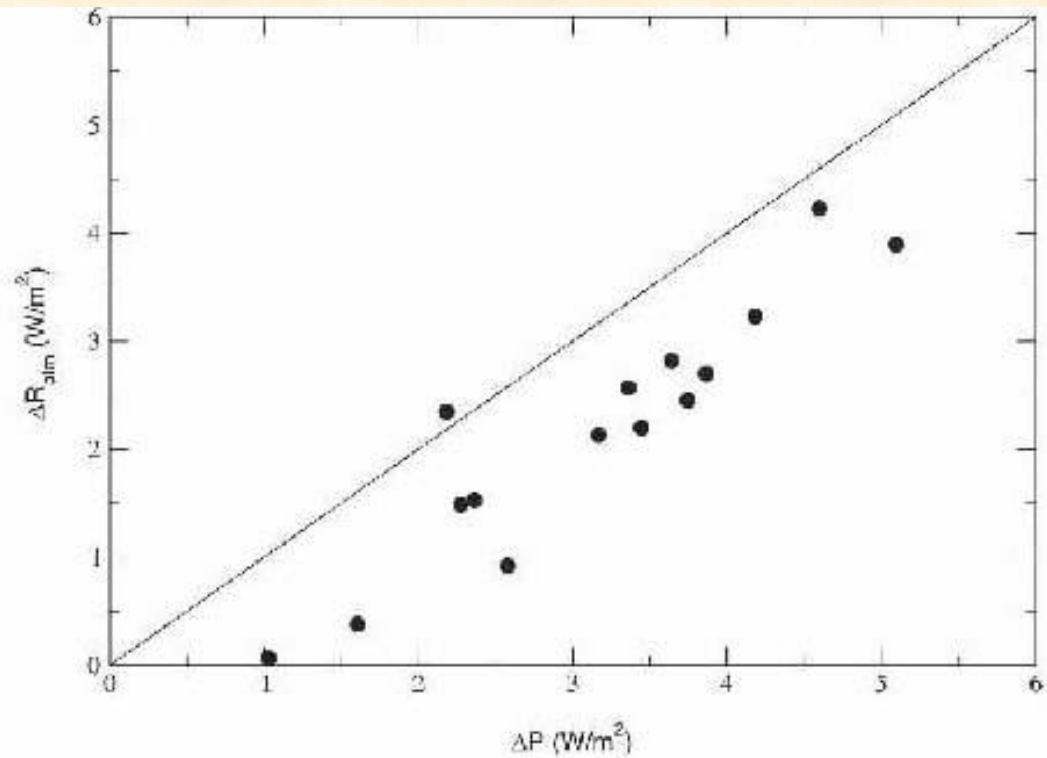
(b) Precipitation vs. Temperature



$\Rightarrow < 0$

\Rightarrow slowing of tropical
circulation \rightarrow
dynamic component

Held and Soden (2006); Vecchi and Soden (2007)



(d) Radiative Cooling vs. Precipitation

Vecchi and Soden (2007)

In global average, $P = E$

$P \approx LW + SW$ (assuming H is small)

$$\frac{\delta P}{P} \quad \text{increases at 1-3\% per } 1^\circ\text{C T}$$

$$\frac{\delta q}{q} \quad \text{increases at 7.5\% per } 1^\circ\text{C T}$$

$$\rightarrow \frac{\delta M}{M} < 0 \quad ?$$

\rightarrow **NO**

Vertically integrated water vapor budget

$$P - E \approx -\langle \nabla \cdot v q \rangle$$

convergence of moisture flux

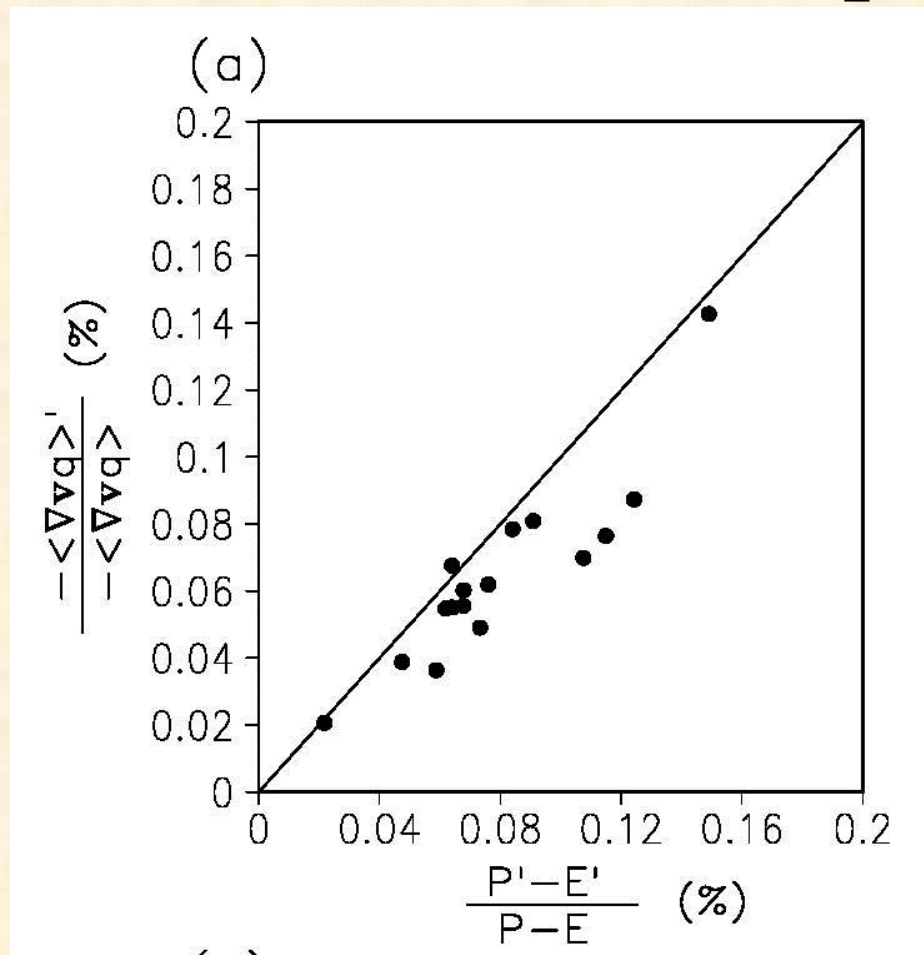
P : precipitation; E : evaporation

q : water vapor (moisture); v : horizontal velocity

ω : vertical velocity; $\langle \rangle$: vertical integration

Vertically integrated water vapor budget

$$\frac{(P - E)'}{P - E} \approx \frac{-\langle \nabla \cdot v q \rangle'}{-\langle \nabla \cdot v q \rangle}$$



$$P' - E' \approx -\langle \omega \partial_p q \rangle' - \langle v \cdot \nabla q \rangle'$$

vertical advection

horizontal advection

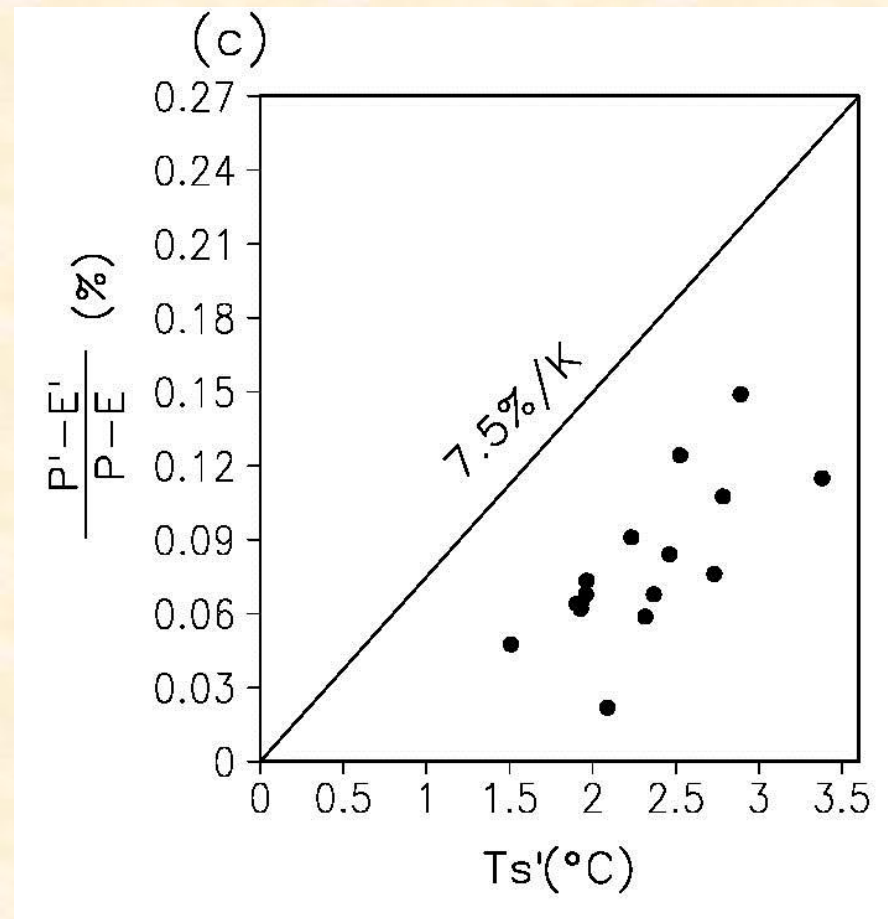
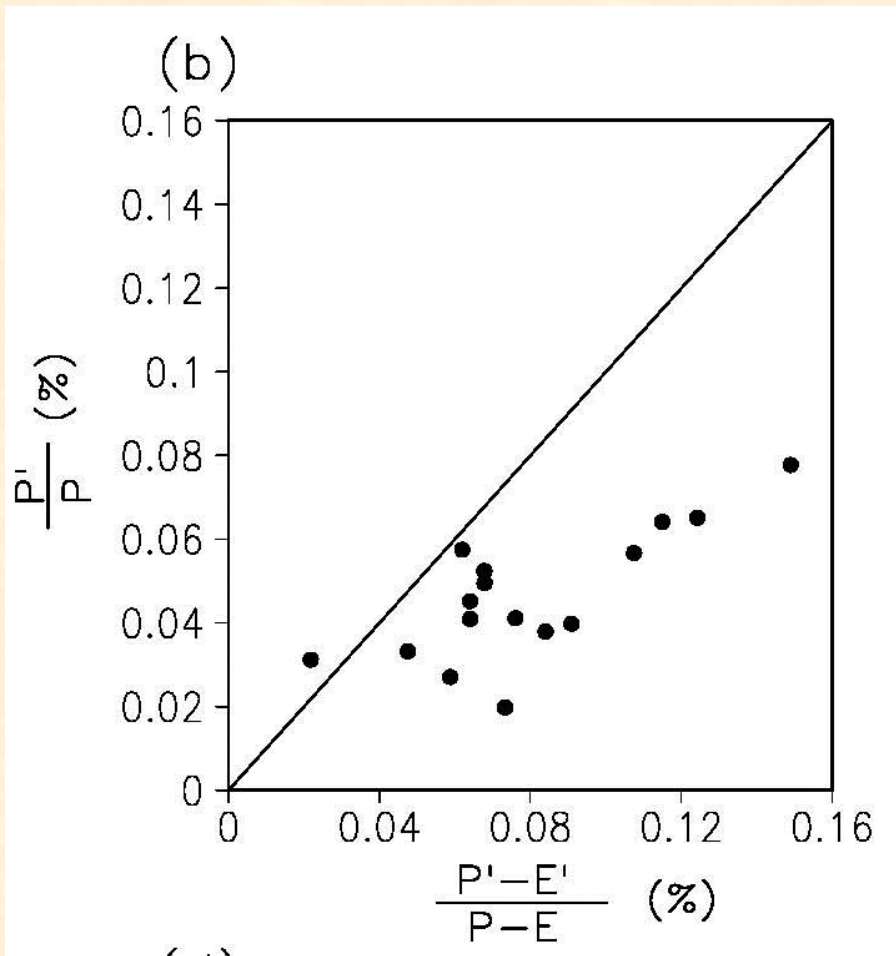
$$\rightarrow P' - E' \approx -\langle \bar{\omega} \partial_p q' \rangle - \langle \omega' \partial_p \bar{q} \rangle - \langle v \cdot \nabla q \rangle'$$

thermodynamic

dynamic

$$\rightarrow \frac{P' - E'}{\bar{P} - \bar{E}} \approx \frac{-\langle \bar{\omega} \partial_p q' \rangle}{-\langle \nabla \cdot v q \rangle} + \frac{-\langle \omega' \partial_p \bar{q} \rangle}{-\langle \nabla \cdot v q \rangle}$$

$$\frac{P'}{\bar{P}} \approx \frac{\delta q}{\bar{q}} + \frac{\delta M}{\bar{M}}$$

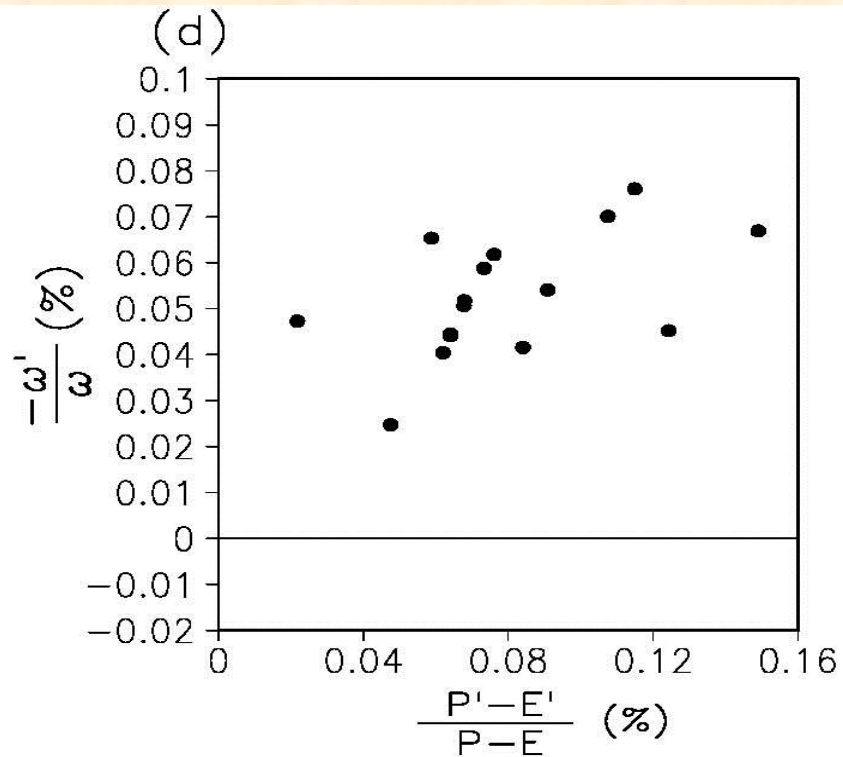


$$\rightarrow \frac{P'}{P} < \frac{(P-E)'}{P-E} < 7.5\%$$

$$\frac{P' - E'}{\bar{P} - \bar{E}} \approx \frac{-\langle \bar{\omega} \partial_p q' \rangle}{-\langle \nabla \cdot v \bar{q} \rangle} + \frac{-\langle \omega' \partial_p \bar{q} \rangle}{-\langle \nabla \cdot v \bar{q} \rangle}$$

$$\frac{P' - E'}{\bar{P} - \bar{E}} < 7.5\% \sim \frac{-\langle \bar{\omega} \partial_p q' \rangle}{-\langle \nabla \cdot v \bar{q} \rangle}$$

→ $\frac{-\langle \omega' \partial_p \bar{q} \rangle}{-\langle \nabla \cdot v \bar{q} \rangle} < 0$: a weakening of tropical circulation



$$\frac{P' - E'}{\bar{P} - \bar{E}} \approx \frac{-\langle \bar{\omega} \partial_p q' \rangle}{-\langle \nabla \cdot v q \rangle} + \frac{-\langle \omega' \partial_p \bar{q} \rangle}{-\langle \nabla \cdot v q \rangle}$$

No constraint

≤ 7.5% in q per 1 °C T



>0 or <0

7.5% in q per 1 °C T

$$\frac{P'}{\bar{P}} \approx \frac{\delta q}{\bar{q}} + \frac{\delta M}{\bar{M}}$$

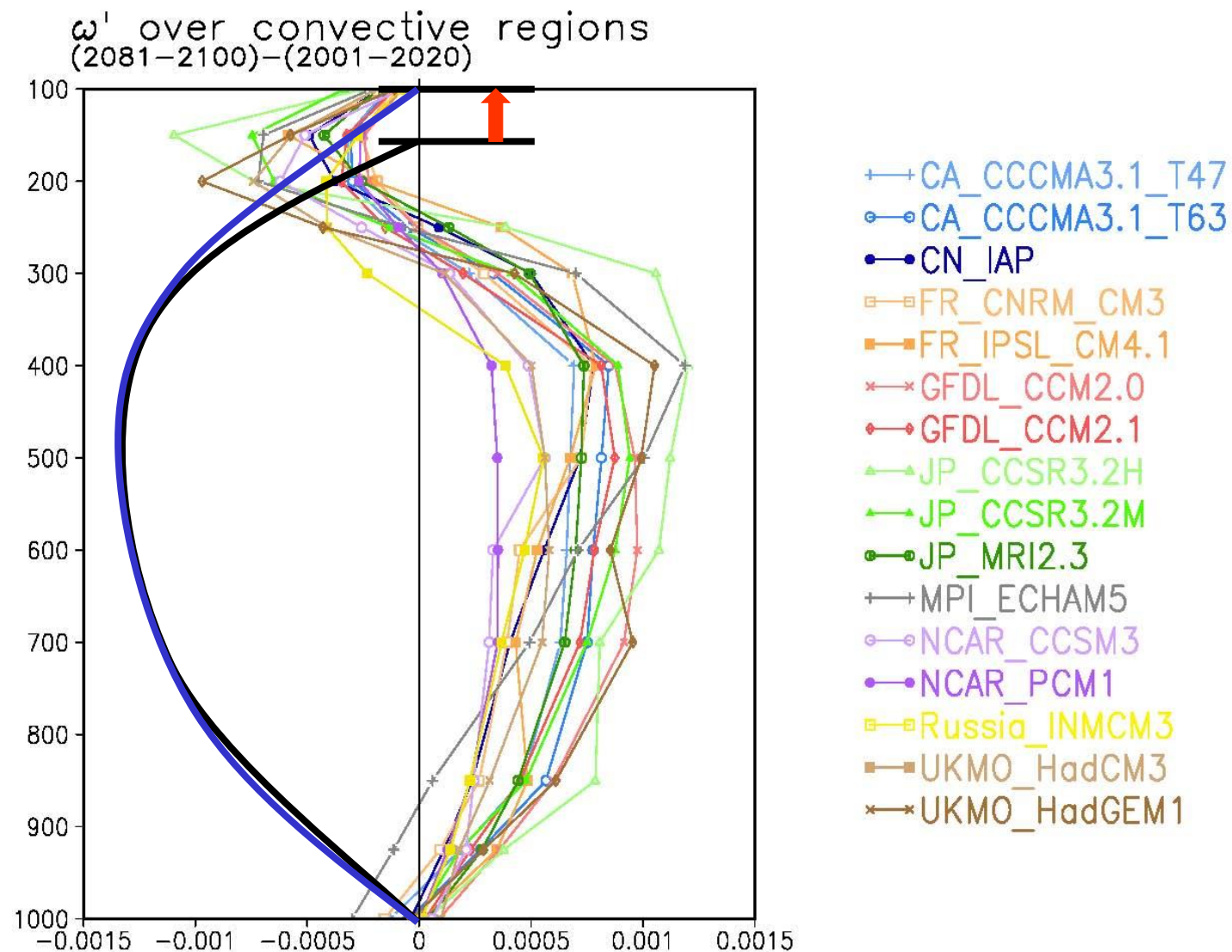


1-3% in P per 1 °C T

<0

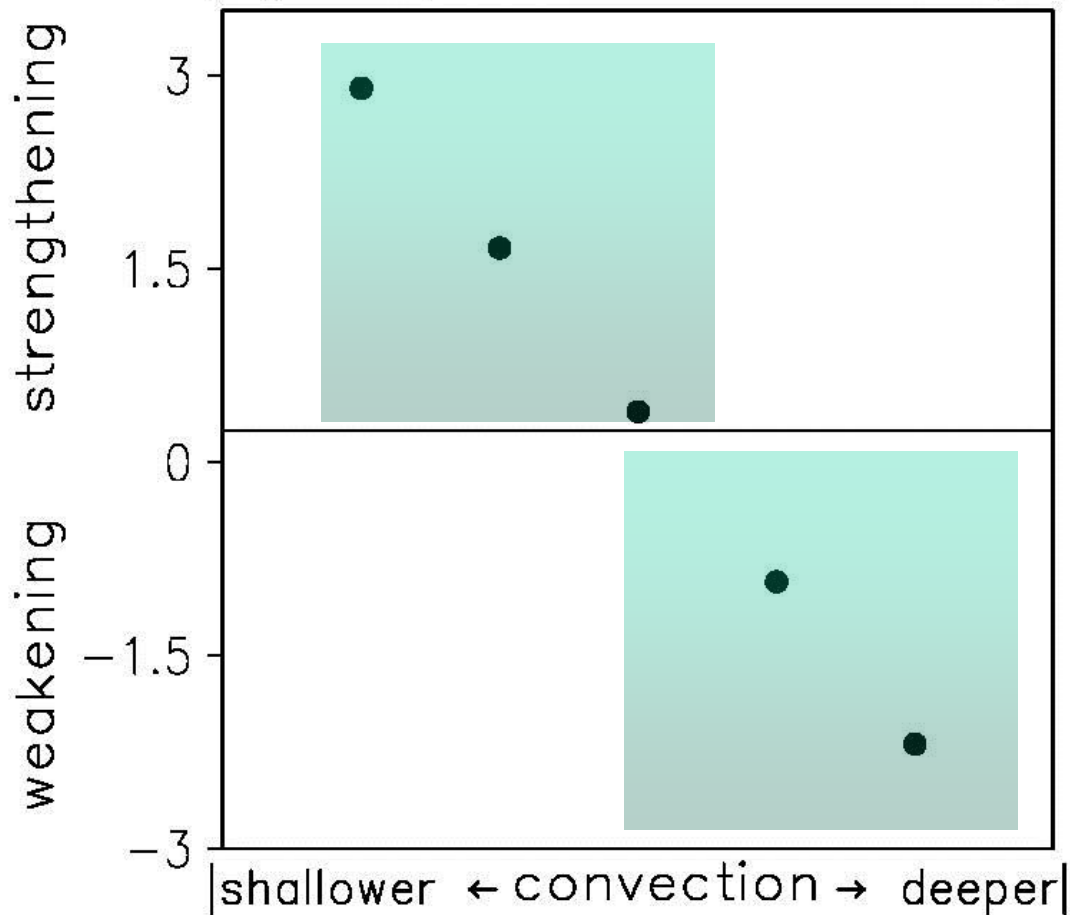
(controlled by energy budget)

Effect of convection depth

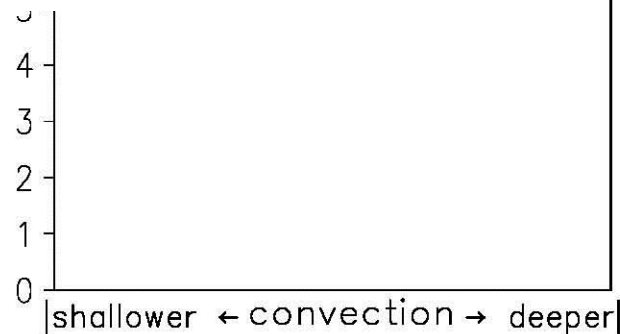
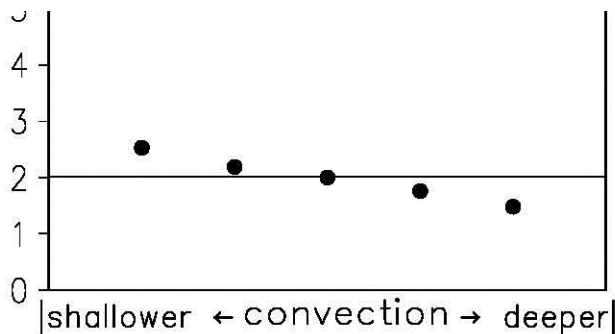
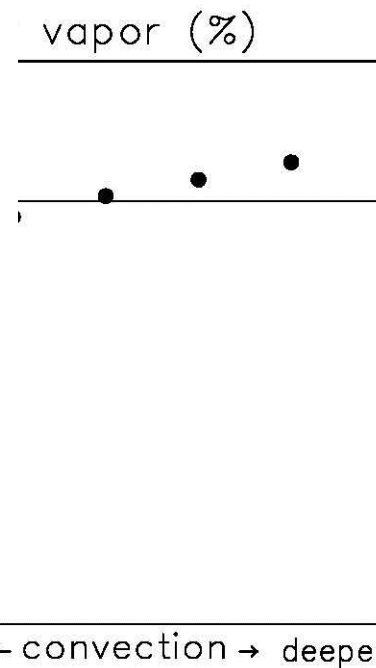


➔ deepening of convection: ~ 2.5–3.4%

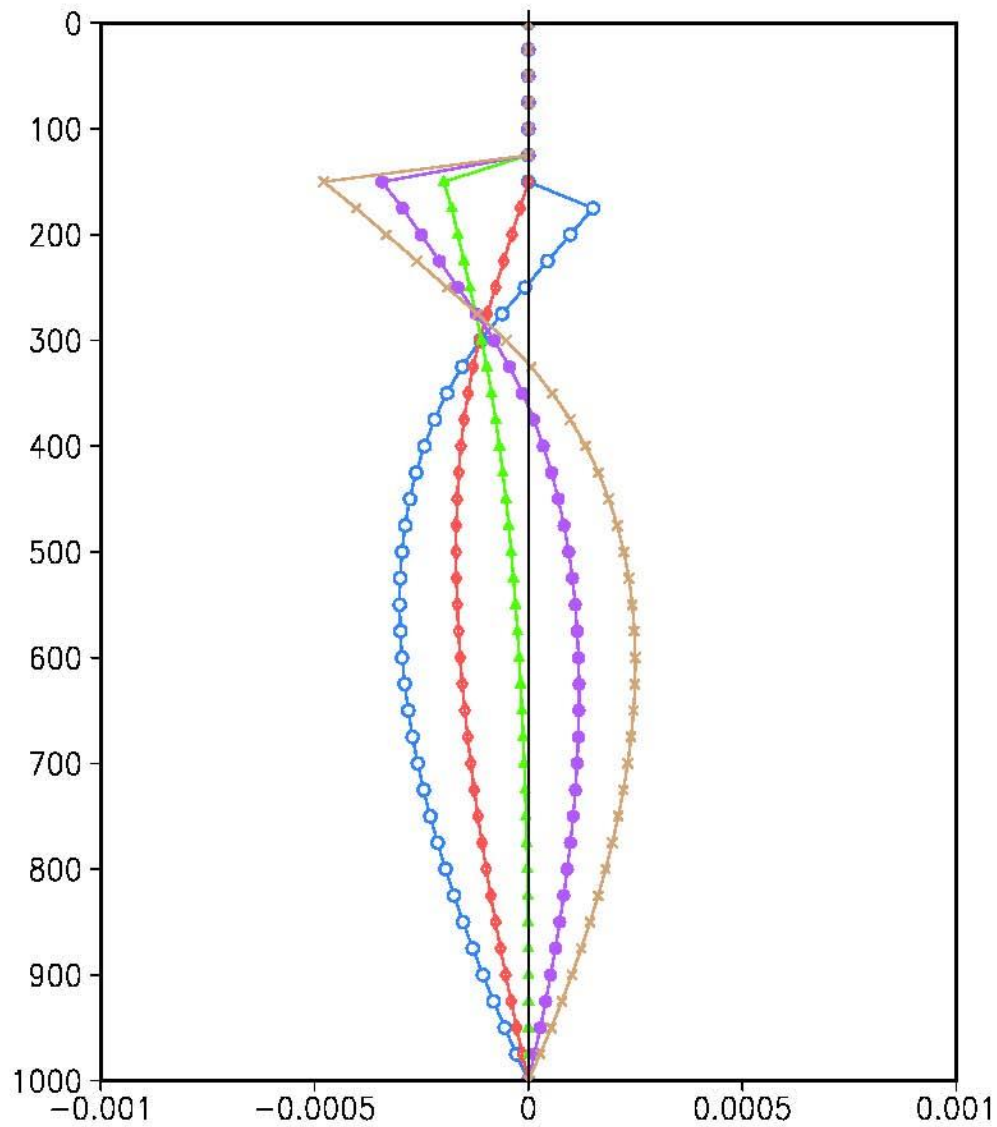
(a) tropical circulation (%)



Convection top:
155 hPa ~ 137 hPa
(-1.2% ~ 3.3%)



ω' over convective regions



155 hPa

150 hPa

145 hPa

141 hPa

137 hPa

shallower←

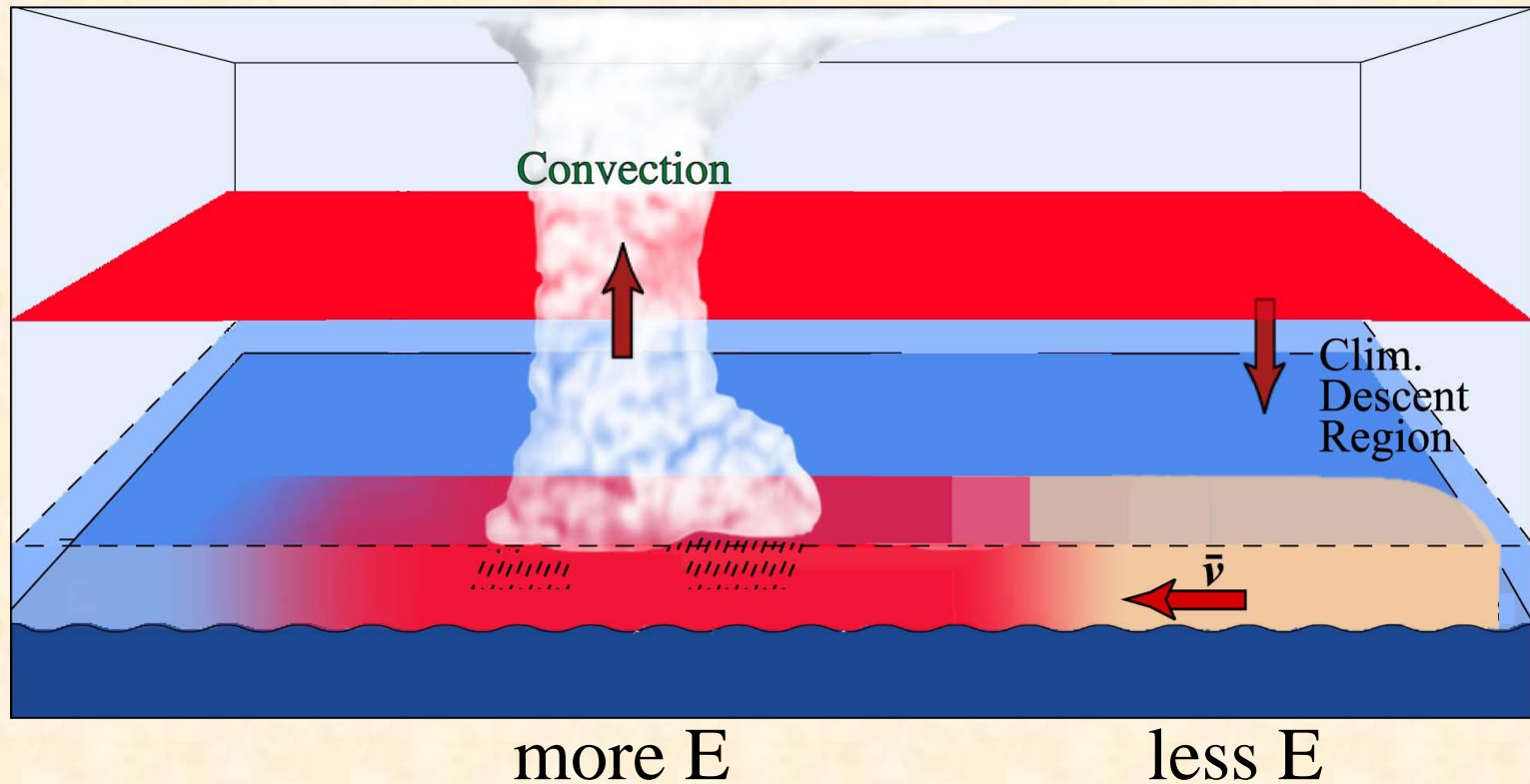
→deeper

term	M_s-1	M_s+0	M_s+1	M_s+2	M_s+3
global P'/\bar{P}	0.0253	0.0219	0.0200	0.0176	0.0148
global E'/\bar{E}	0.0245	0.0217	0.0200	0.0181	0.0156
global q'/\bar{q}	0.0695	0.0724	0.0761	0.0790	0.0821
$\omega'/\bar{\omega}$ at 500 hPa	0.0408	0.0166	-0.0072	-0.0287	-0.0492
$P' - E'/\bar{P} - \bar{E}$	0.0906	0.0695	0.0476	0.0284	0.0088
$-\langle \nabla \cdot \mathbf{v}q \rangle' / -\langle \nabla \cdot \bar{\mathbf{v}}\bar{q} \rangle$	0.0906	0.0695	0.0478	0.0285	0.0089
$-\langle \mathbf{v} \cdot \nabla q \rangle' / -\langle \nabla \cdot \bar{\mathbf{v}}\bar{q} \rangle$	-0.0111	-0.0063	-0.0039	-0.0003	0.0018
$-\langle \omega \partial_p q \rangle' / -\langle \nabla \cdot \bar{\mathbf{v}}\bar{q} \rangle$	0.1017	0.0758	0.0517	0.0288	0.0221
$-\langle \bar{\omega} \partial_p q' \rangle / -\langle \nabla \cdot \bar{\mathbf{v}}\bar{q} \rangle$	0.0531	0.0572	0.0621	0.0638	0.0662
$-\langle \omega' \partial_p \bar{q} \rangle / -\langle \nabla \cdot \bar{\mathbf{v}}\bar{q} \rangle$	0.0418	0.0183	-0.0032	-0.0249	-0.0459
P'/\bar{P}	0.0376	0.0305	0.0252	0.0196	0.0153
E'/\bar{E}	-0.0099	-0.0044	0.0050	0.0117	0.0211

$$\frac{P' - E'}{\bar{P} - \bar{E}} \approx \frac{-\langle \bar{\omega} \partial_p q' \rangle}{-\langle \nabla \cdot \bar{\mathbf{v}}\bar{q} \rangle} + \frac{-\langle \omega' \partial_p \bar{q} \rangle}{-\langle \nabla \cdot \bar{\mathbf{v}}\bar{q} \rangle}$$

thermodynamic
dynamic

Deeper convection



$$P' \approx E' - \langle \nabla \cdot v q \rangle'$$

- Reduced upward motion; Less convergence of moisture flux
- more evaporation

Vertically integrated moist static energy budget

$$\langle \omega' \partial_p \bar{h} \rangle \approx -\langle \bar{\omega} \partial_p h' \rangle - \langle \mathbf{v} \cdot \nabla (T + q) \rangle' + F^{net}$$

shallower ←

→ deeper

term	M_s-1	M_s+0	M_s+1	M_s+2	M_s+3	
$\langle \omega' \partial_p \bar{h} \rangle / \langle \bar{\omega} \partial_p h \rangle$	0.0375	0.0149	-0.0067	-0.0303	-0.0501	ascent
$-\langle \bar{\omega} \partial_p h' \rangle / \langle \bar{\omega} \partial_p h \rangle$	0.1259	0.0819	0.0368	-0.0030	-0.0464	stability
$-\langle \mathbf{v} \cdot \nabla (q + T) \rangle' / \langle \bar{\omega} \partial_p h \rangle$	-0.0401	-0.0412	-0.0562	-0.0542	-0.0648	
$F^{net} / \langle \bar{\omega} \partial_p h \rangle$	-0.0011	0.0092	0.0340	0.0453	0.0691	

➔ The deeper (shallower) convection,
the more stable, larger values, (unstable, smaller
values) the atmosphere

Under quasi-equilibrium closure

$$\langle \omega \partial_p h \rangle = M \nabla \cdot v_1$$

where

$$M = -\langle \Omega \partial_p h \rangle \quad \text{gross moist stability}$$

$$\nabla \cdot v_1 \quad \text{divergence (baroclinic winds)}$$

Ω : typical profile of vertical velocity for deep convection

horizontal advection

$$\langle \omega' \partial_p \bar{h} \rangle \approx -\langle \bar{\omega} \partial_p h' \rangle - \langle v \cdot \nabla (T + q) \rangle' + F^{net'}$$

atmospheric
stability

net energy input

→

$$\nabla \cdot v_1' \approx \frac{1}{\bar{M}} [-M \nabla \cdot \bar{v}_1 - \langle v \cdot \nabla (T + q) \rangle' + F^{net'}]$$

→

$$\frac{\nabla \cdot v_1'}{\nabla \cdot \bar{v}_1} \approx -\frac{M'}{\bar{M}}$$

Gross moist stability

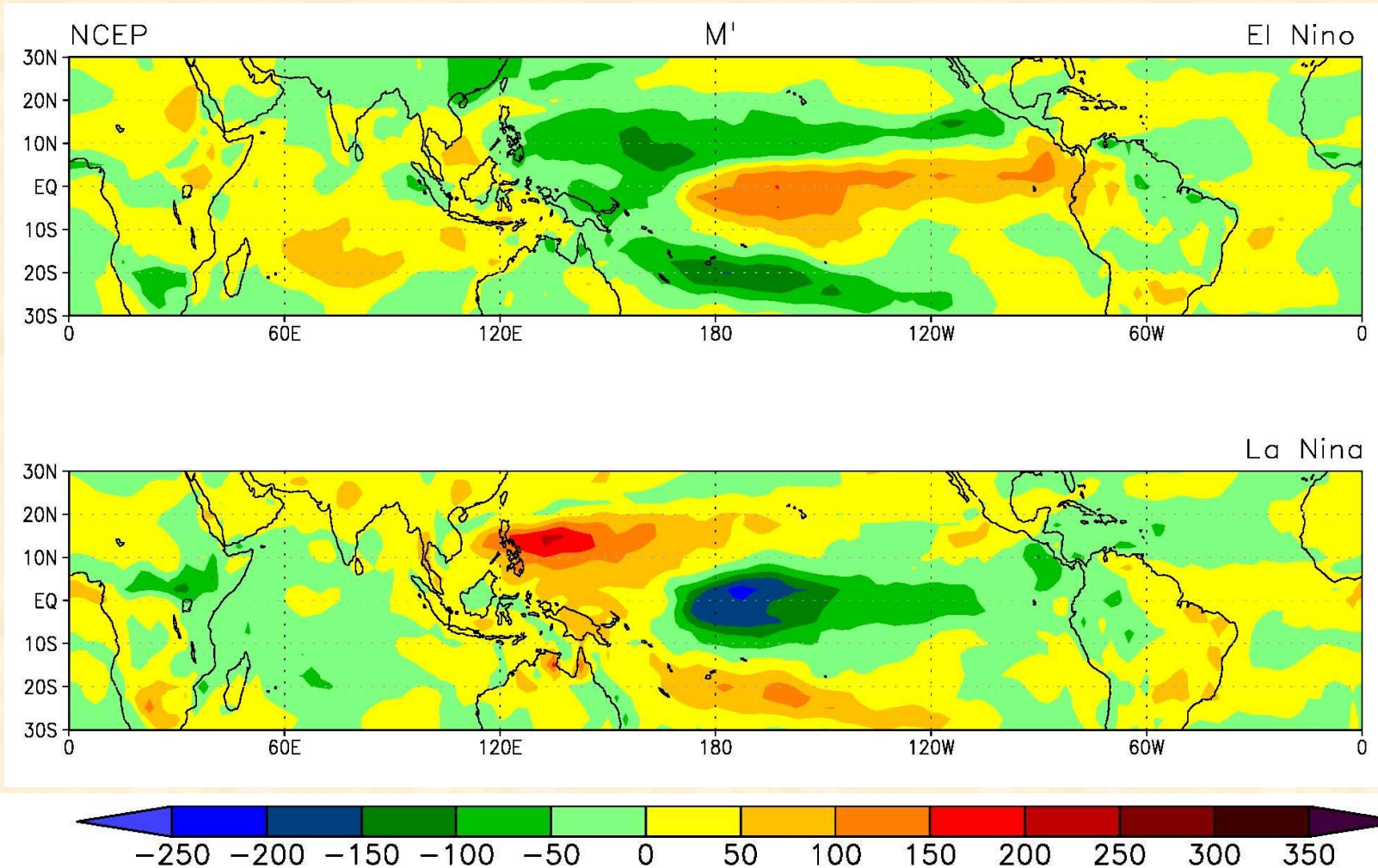
$$M = -\langle \Omega \partial_p h \rangle$$

$$= M(T, q, p_t)$$

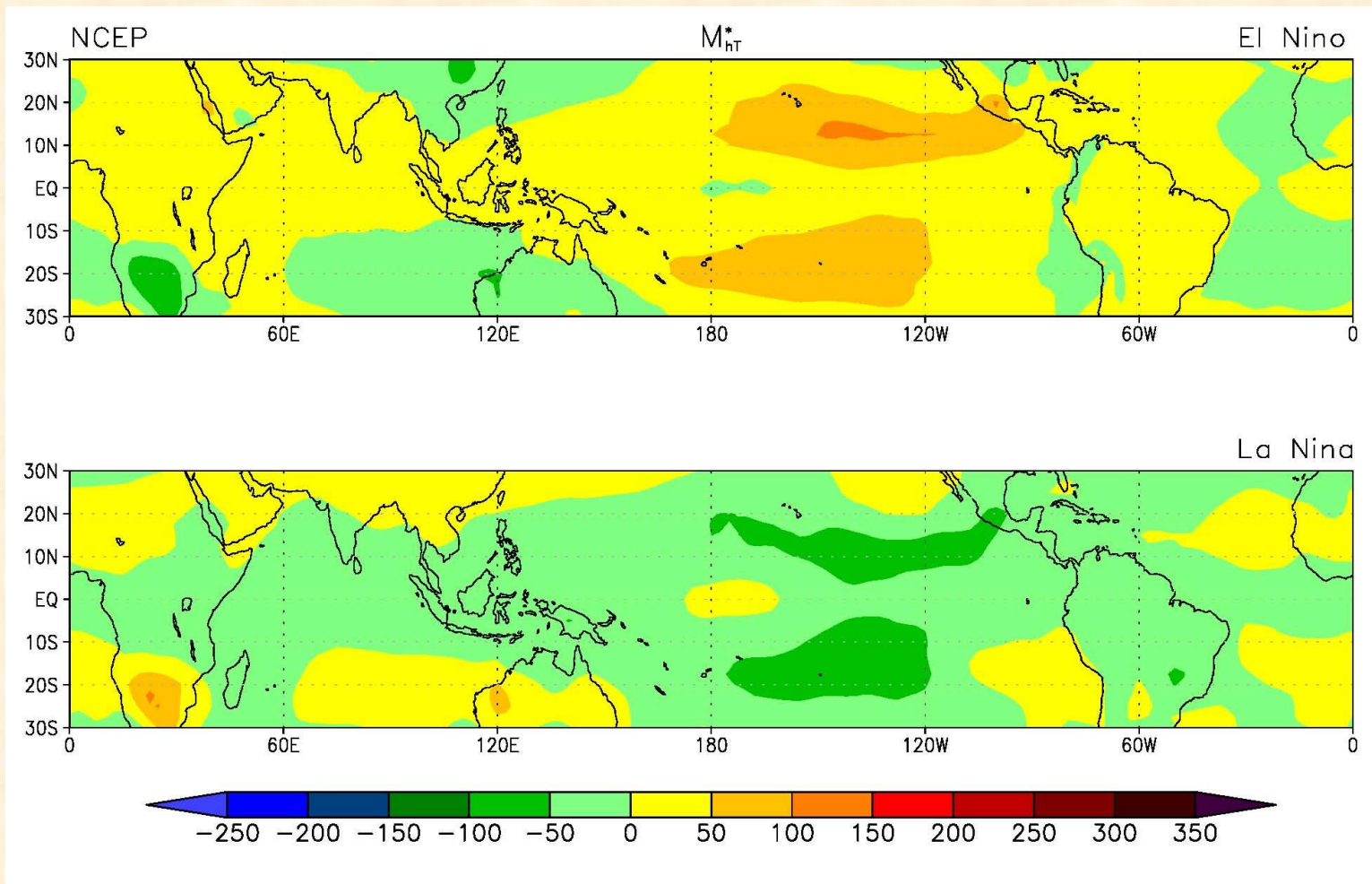
$$= M(\bar{T}, \bar{q}, \bar{p}_t) + M(T', \bar{q}, \bar{p}_t) + M(\bar{T}, q', \bar{p}_t) + M(\bar{T}, \bar{q}, p'_t) + \Delta M$$

$$= \tilde{M} + M_{hT}^* + M_{hq}^* + M_{pt}^* + \Delta M$$

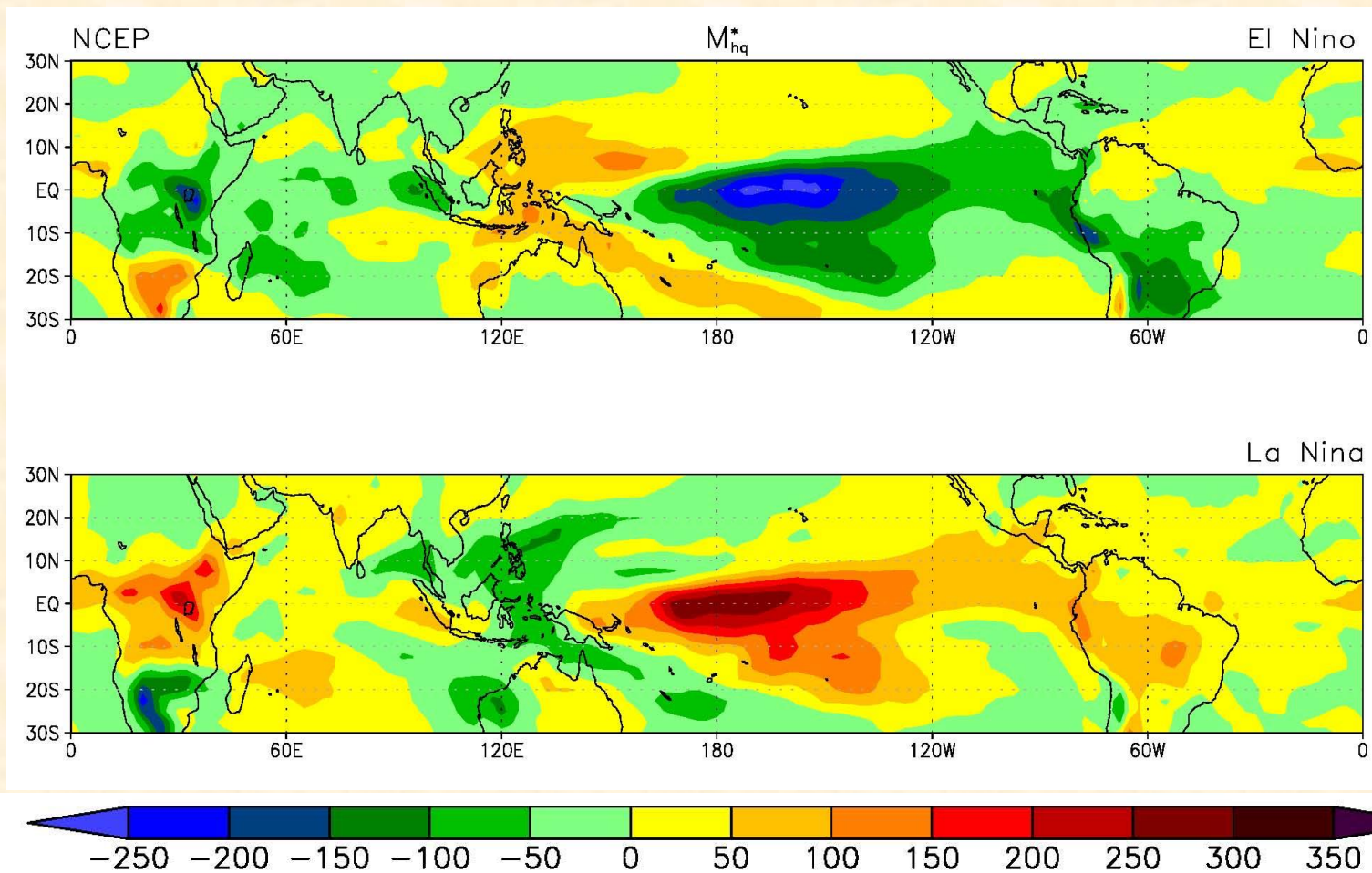
ENSO



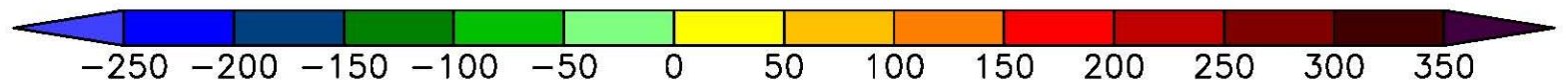
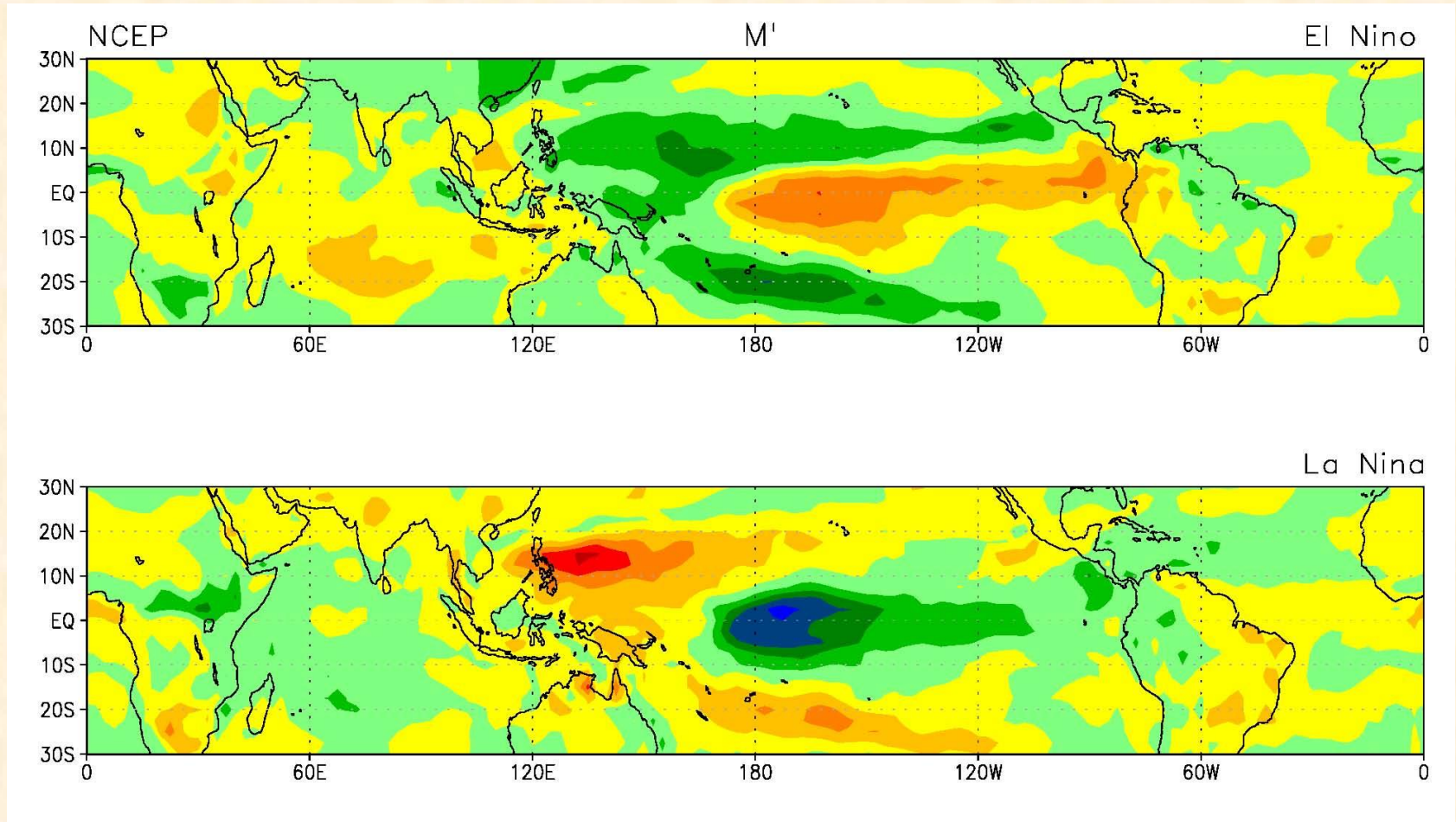
$$M_{hT}^*$$



$$M_{hq}^*$$



$$M_{pt}^*$$



Conclusion

- Slower increase of rainfall and faster increase of water vapor → no guarantee for weakening of tropical circulation
- Effect of convection depth: the deeper (shallower) convection, the weaker (stronger) the circulation
→ inconsistent among observed strength of tropical convection
- Gross moist stability M : an index to measure atmospheric stability

Chou and Chen, 2010, J. Climate, 23, 3019-3030.